

For further research, by using the concept of rough rings and rough ideals, concepts related to rough quotient rings can be obtained. Furthermore, by using the concept of rough rings, we can construct a notion of rough rings homomorphism and rough rings isomorphism.

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